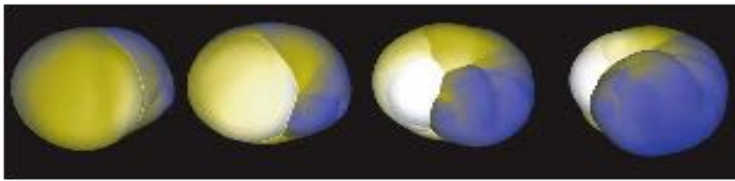
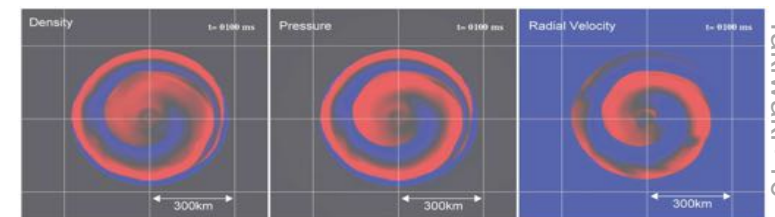
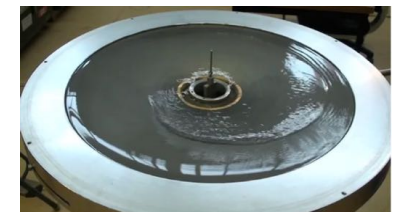
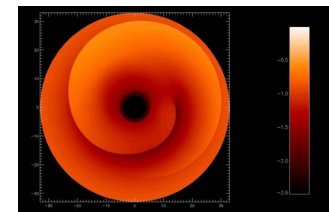
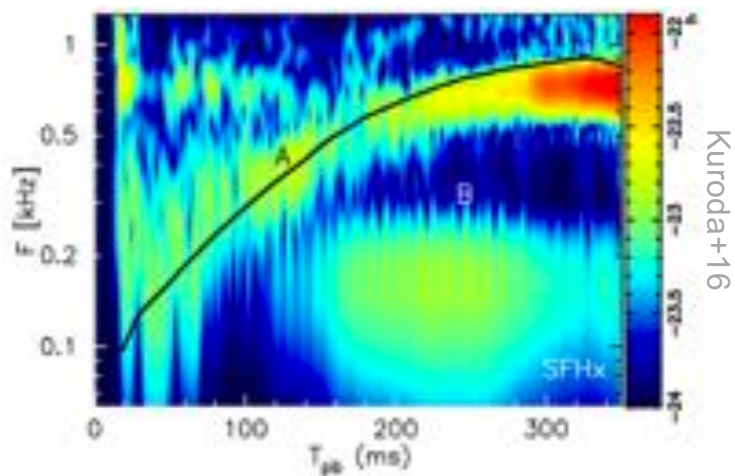
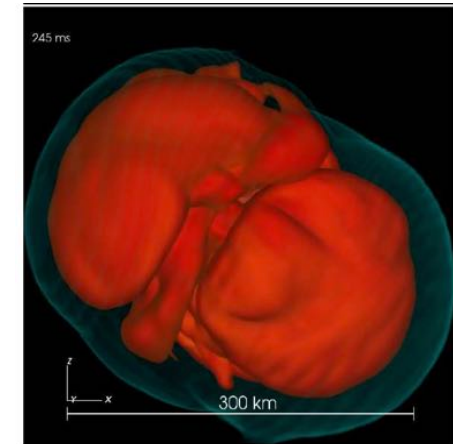
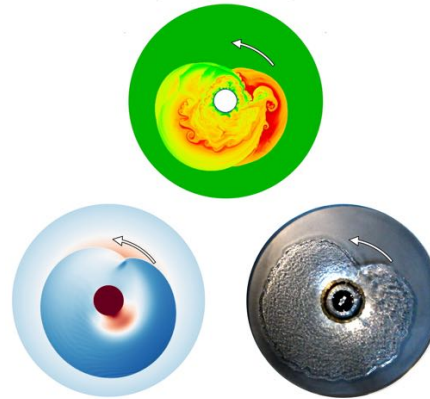


Non axisymmetric instabilities during stellar core collapse illustrated by a shallow-water experiment

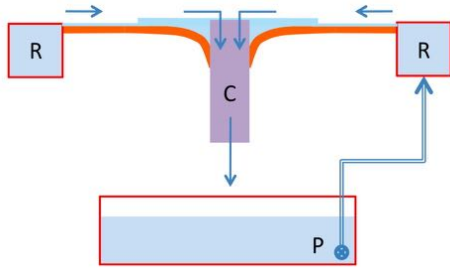


Blondin & Mezzacappa 07

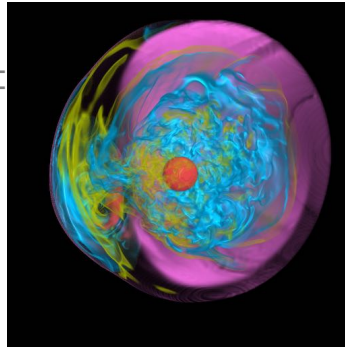


SWASI: an experimental analogue of SASI

Shallow Water Analogue of a Shock Instability



Blondin & Mezzacappa 07



adiabatic gas

$$c_s^2 \equiv \frac{\gamma P}{\rho}$$

$$\Phi \equiv -\frac{GM_{\text{ns}}}{r}$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho v) = 0$$

$$\frac{\partial v}{\partial t} + (\nabla \times v) \times v + \nabla \left(\frac{v^2}{2} + \frac{c_s^2}{\gamma - 1} + \Phi \right) = \frac{c_s^2}{\gamma} \nabla S$$

Inviscid shallow water is analogue to an isentropic gas $\gamma=2$

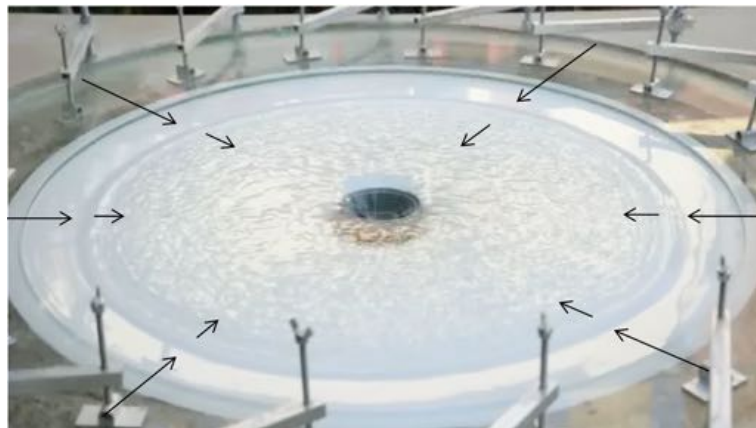
St Venant

$$c_{\text{sw}}^2 \equiv gH$$

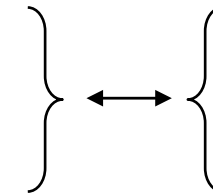
$$\Phi \equiv gH_\Phi$$

$$\frac{\partial H}{\partial t} + \nabla \cdot (Hv) = 0$$

$$\frac{\partial v}{\partial t} + (\nabla \times v) \times v + \nabla \left(\frac{v^2}{2} + c_{\text{sw}}^2 + \Phi \right) = 0$$



acoustic waves
shock wave
pressure



surface waves
hydraulic jump
depth

expected scaling

$$\frac{t_{\text{ff}}^{\text{sh}}}{t_{\text{ff}}^{\text{jp}}} \equiv \left(\frac{r_{\text{sh}}}{r_{\text{jp}}} \right) \left(\frac{r_{\text{sh}} g H_{\text{jp}}}{GM_{\text{NS}}} \right)^{\frac{1}{2}} \sim 10^{-2}$$

shock radius $\times 10^{-6}$

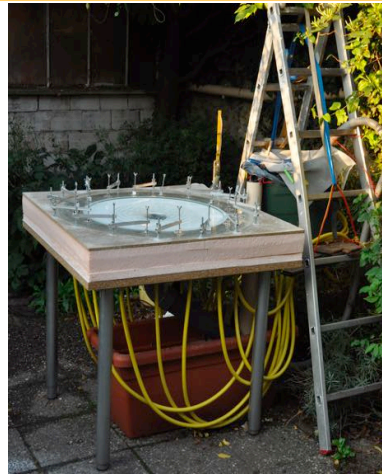
200 km \rightarrow 20 cm

oscillation period $\times 10^2$

30 ms \rightarrow 3 s

SWASI: simple as a garden experiment

November 2010



October 2010



June 2010



May 2010

February 2012



November 2013



June 2014

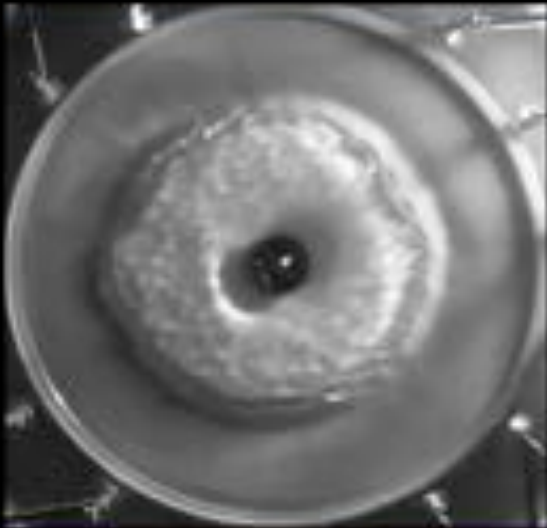


February 2017

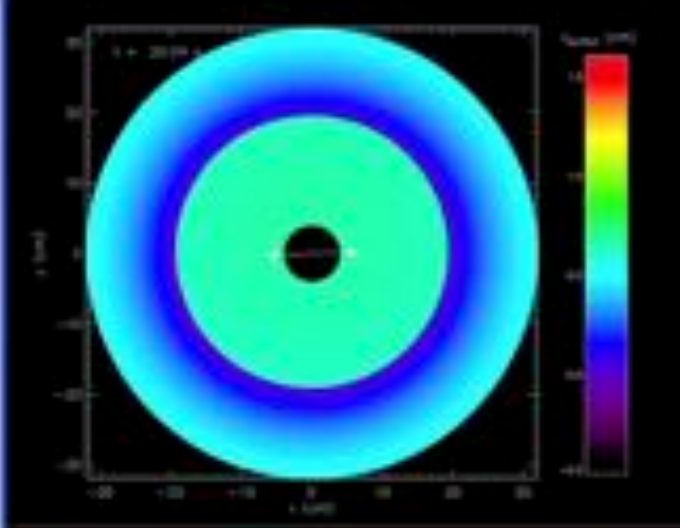
Dynamics of water in the fountain

Dynamics of the gas in the supernova core

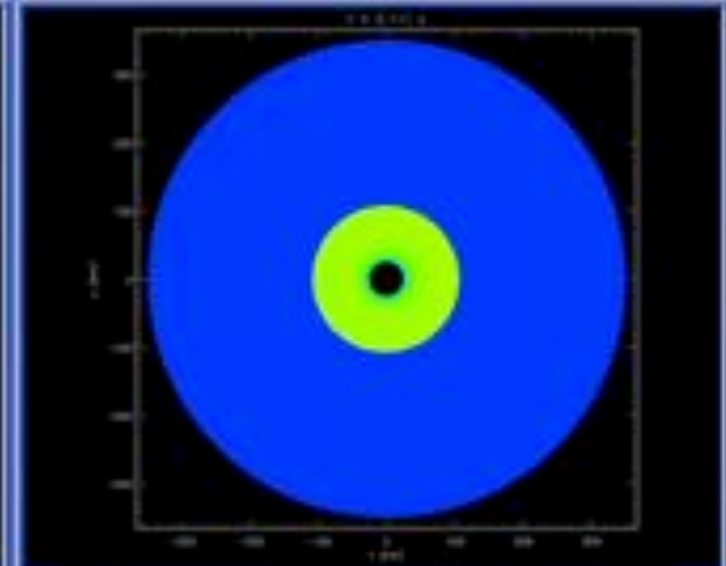
diameter 40cm ← 1 000 000 x bigger → diameter 400km
3s/oscillation ← 100 x faster → 0.03s/oscillation



Expérience hydraulique

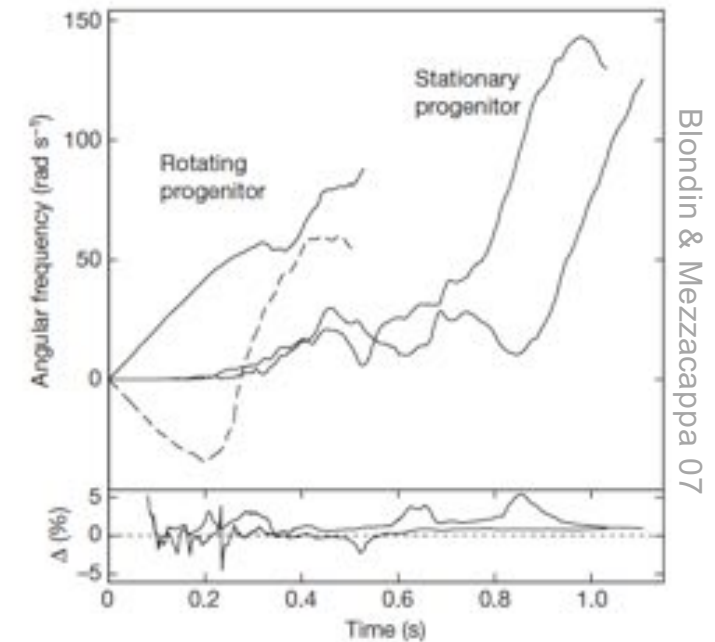


Simulation numérique de l'expérience hydraulique



*Simulation numérique de l'onde de choc
dans le cœur de la supernova*

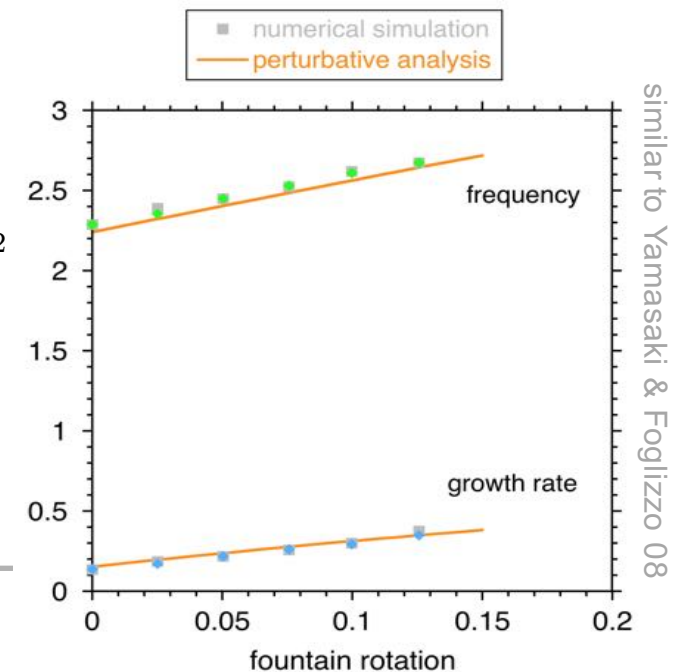
Rotating progenitor: accreted angular momentum changes its sign as SASI grows



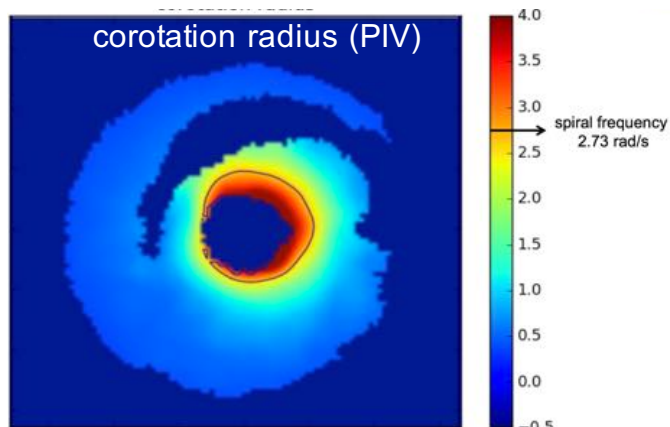
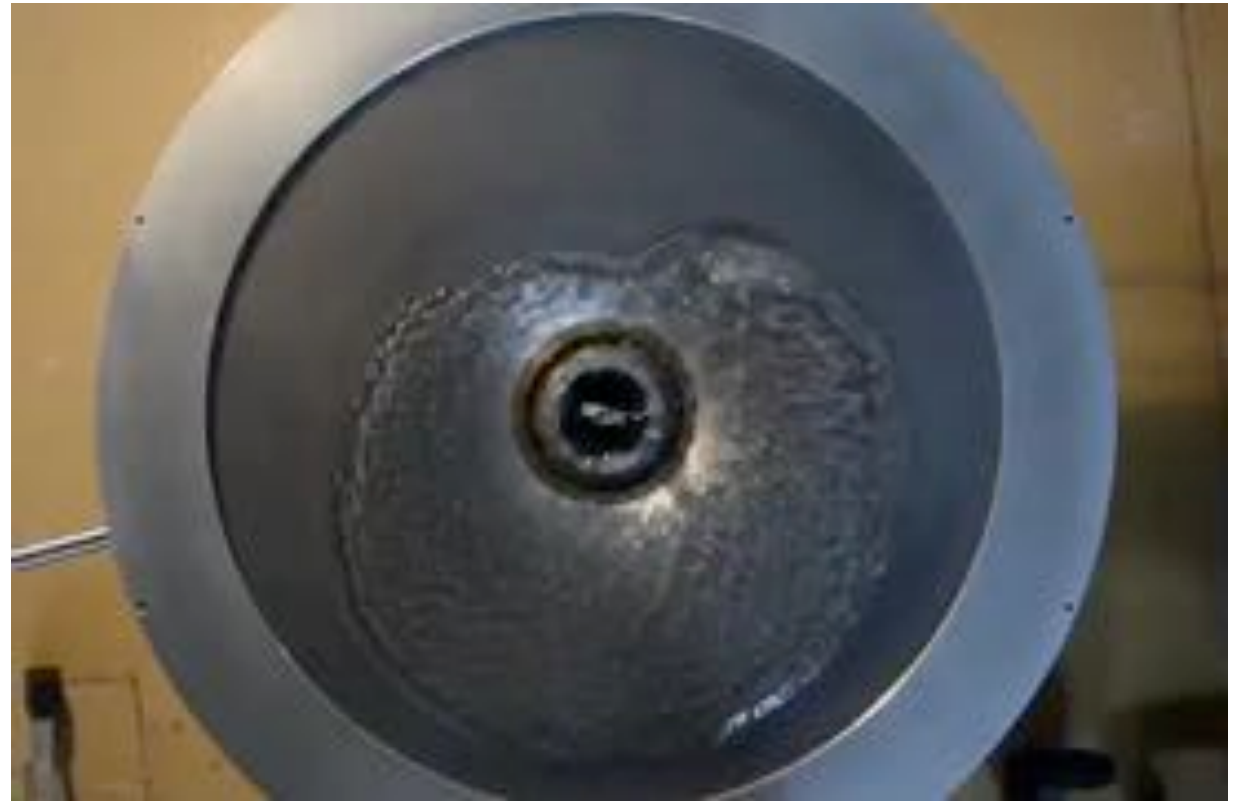
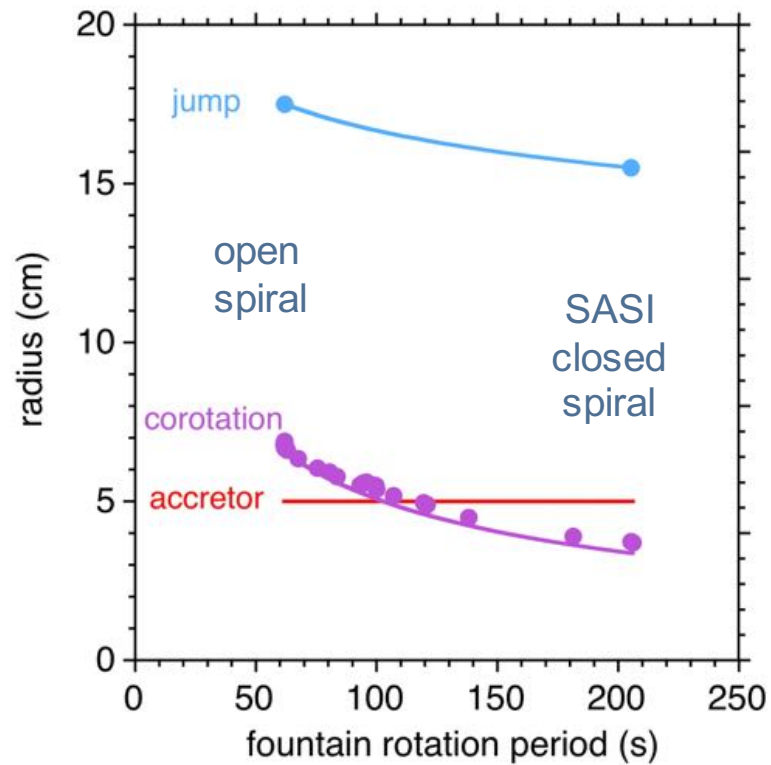
-significant shear even when the centrifugal force $\Omega^2 R$ is weak $\frac{\Omega}{\Omega_{NS}} \propto \left(\frac{R_{NS}}{R}\right)^2$

-the prograde mode is favoured by differential rotation as in shocked accretion:
can produce counter rotating pulsars up to 30Hz

Blondin & Mezzacappa 07, Yamasaki & Foglizzo 08, Kazeroni+17



Increasing the rotation rate: continuous transition from SASI to the corotation instability



the rotation period is gradually decreased (205s \rightarrow 62s)

the flow rate is gradually decreased (1.1 L/s \rightarrow 0.59 L/s)

Unexpectedly robust spiral shock driven at the corotation radius when the inner rotation rate reaches 20% Kepler (low $T/|W|=0.02$)



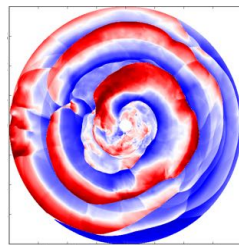
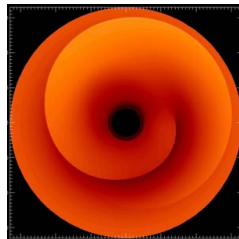
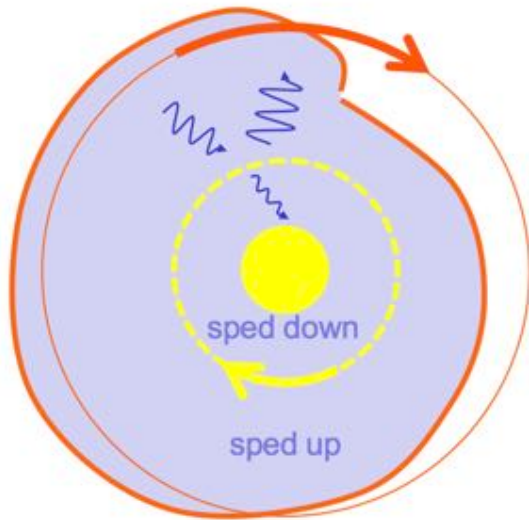
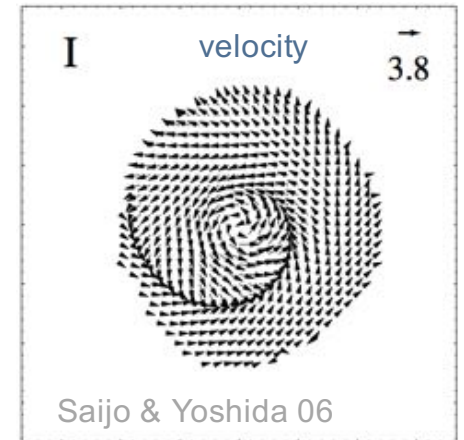
Spiral instability with a weak shock

Radial accretion enforces
differential rotation

$$\frac{\Omega}{\Omega_{\text{NS}}} \propto \left(\frac{R_{\text{NS}}}{R} \right)^2$$

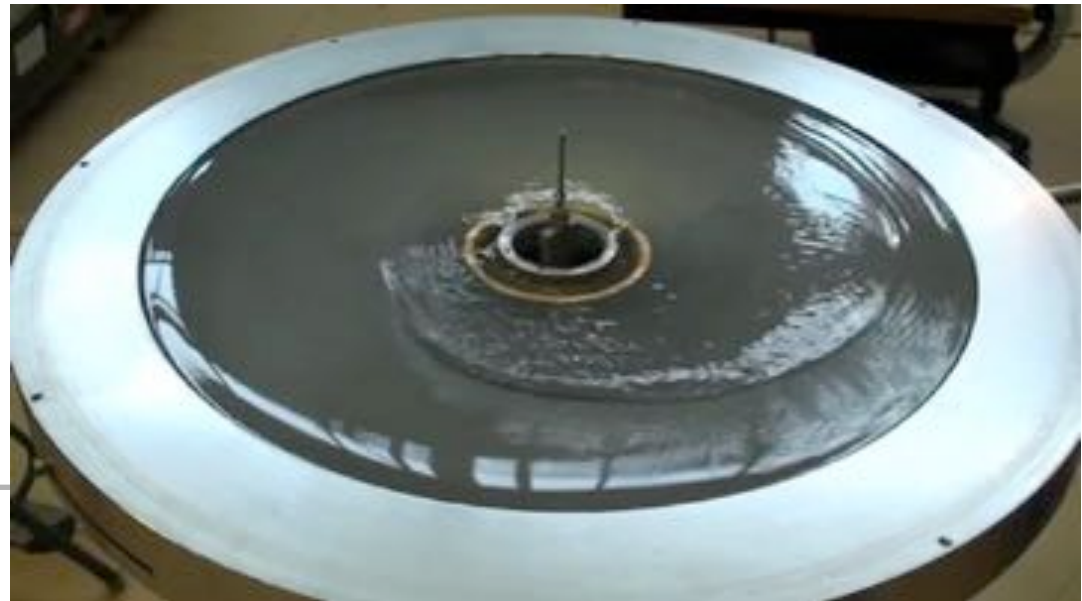
Analogue to the "low $T/|W|$
instability" of a neutron star
rotating differentially

(Shibata+02,03, Saijo+03,06,
Watts+05, Corvino+10,
Passamonti & Andersson 15)



Instability mechanism: interaction of a corotation radius with
acoustic waves (Papaloizou & Pringle 84, Goldreich & Narayan 85)

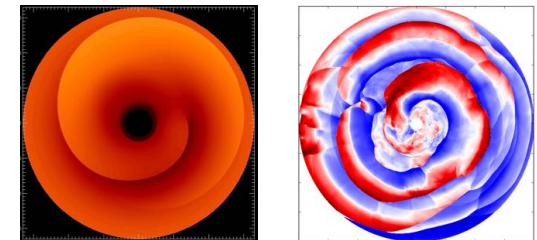
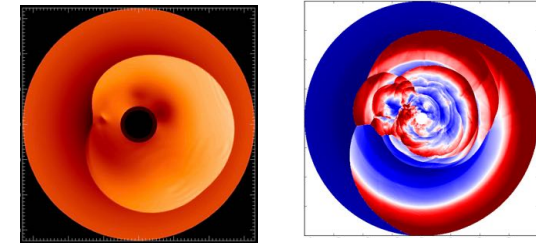
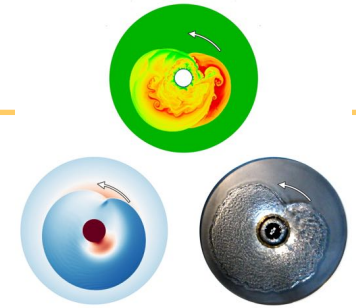
Spiral instability with subsonic accretion



Conclusions

Two core collapse instabilities captured in a hydraulic experiment

- an intuitive approach to multi-D processes that produce GW
- experimental results confirmed by a shallow water numerical model
- first** experimental confirmation that spiral SASI can produce a counter-spinning neutron star
- first** experimental demonstration of the 'low $T/|W|$ ' instability
- the corotation instability 'low $T/|W|$ ' connects smoothly to SASI



Cylindrical gas dynamics suggests that (Kazeroni+17)

- SASI can account for pulsar rotation rates up to $\sim 30\text{Hz}$
- for rotation rates $> 100\text{Hz}$ the corotation instability decreases the pulsar spin by $< 30\%$

